



Supplementary Materials for
**Observation of the transition state for pressure-induced $\text{BO}_3 \rightarrow \text{BO}_4$
conversion in glass**

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Supplementary Materials:

Materials and Methods

The borosilicate glass Corning code 7059 was chosen for the present study. This glass has a chemical composition of (mol%) 12.5% BaO, 8.5% Al₂O₃, 16% B₂O₃, and 63% SiO₂ and a calorimetric glass transition temperature T_g of ~ 950 K (18). Drawn sheets (150.0 x 150.0 x 1.1 mm) of this glass were obtained from Corning Incorporated. Samples were core drilled from a glass sheet to obtain rods of ~ 1 mm diameter by 3 mm length for high-pressure studies. The *in situ* high-pressure ¹¹B wideline NMR spectroscopic measurements were carried out using a home-built high-pressure NMR probe (see below, for details) in a horizontal bore (bore inner diameter 180 mm) 7T Bruker imaging magnet equipped with a Bruker BioSpec spectrometer system operating at a ¹¹B Larmor frequency of 96 MHz. Single-pulse ¹¹B NMR spectra were collected at various pressures ranging between ambient and 2 GPa, using a $\pi/8$ solids pulse (0.4 μ s) with a recycle delay of 1 s. Approximately 10,000 free induction decays were averaged and Fourier transformed to obtain each spectrum.

Two samples core drilled from the same glass sheet were subjected to high P-T conditions in a 6-8 multi anvil apparatus for *ex situ* high-resolution ¹¹B magic-angle-spinning (MAS) NMR spectroscopic measurements. One of the samples was taken to 8 GPa at ambient temperature and equilibrated for 12 hours before decompression at a rate of 4 GPa/h. Another sample was taken to 2 GPa and subsequently heated to 1000 K, equilibrated at that temperature for 2 hours followed by thermal quenching at 50 K/s and subsequently decompression at 4 GPa/h. ¹¹B MAS NMR spectra of these two samples and of the as-received glass were collected using a 11.7T magnet (Bruker) and a spectrometer (Bruker Avance500) operating at a ¹¹B

Larmor frequency of 160.4 MHz. Single-pulse ^{11}B NMR spectra were collected using a MAS probe (Doty Inc.) with a $\pi/10$ solids pulse (0.25 μs) and a recycle delay of 0.25 s. Crushed samples were taken in a ZrO_2 rotor and were spun at 12 kHz. Approximately 3000 to 12000 free induction decays were averaged and Fourier transformed to obtain each spectrum.

Table S1. ^{11}B NMR parameters for BO_3 and BO_4 sites obtained from simulation of the ^{11}B wide-line NMR spectra obtained *in situ* at various pressures.

Pressure	Coordination Environment	C_Q (MHz) (± 0.05)	η	δ_{iso} (ppm)	FWHM (ppm)	Relative fraction ($\pm 2\%$) [*]
0.1 MPa	BO_3	2.70	0.0	17.3	–	75
	BO_4	~ 0.00	–	0.5	32.5	25
1.0 GPa	BO_3	2.73	0.0	19.0	–	75
	BO_4	~ 0.00	–	0.4	33.0	25
1.6 GPa	BO_3	2.73	0.0	19.9	–	76
	BO_4	~ 0.00	–	0.4	34.5	24
2.0 GPa	BO_3	2.75	0.0	20.6	–	75
	BO_4	~ 0.00	–	0.5	31.4	25

^{*}Relative error between spectra

Table S2. ^{11}B NMR parameters for BO_3 and BO_4 sites obtained from simulation of the ^{11}B MAS NMR spectra.

Sample	Coordination Environment	C_Q (MHz) (± 0.05)	η	δ_{iso} (ppm)	FWHM (ppm)	Relative fraction ($\pm 1\%$) [*]
As-received glass	BO_3	2.60	0.0	16.2	–	76
	BO_4	~ 0.00	–	0.5	2.9	24
Quenched from 2 GPa and 1000K	BO_3	2.67	0.0	15.9	–	70
	BO_4	~ 0.00	–	-0.3	3.3	30
Quenched from 8 GPa and 298 K	BO_3	2.70	0.0	16.4	–	74
	BO_4	~ 0.00	–	0.3	3.0	26

*Relative error between spectra

High-pressure NMR Probe

The *in situ* high-pressure NMR experiments were carried out using a custom-built NMR probe where the glass sample was pressurized using a cylindrical high-pressure cell (*EasyCell 30*, Almax-Easylab) that was configured for NMR measurements (19). A simple cross-sectional schematic of the cell configuration is shown in Fig. S1. The cell sleeve consists of an outer and an inner shell made of non-magnetic Cu-Be alloy and MP35N superalloy, respectively (20). The 7059 glass plate was core drilled to obtain rods ~ 1 mm diameter by 3 mm length and an NMR coil was then fitted around the sample rod and the leads were epoxied into a pressure cell feed-through (Figs. S1,S2). The sample/coil is fitted inside a Teflon[®] cylindrical cup filled with Daphne 7373 paraffin industrial oil as a pressure transmitting fluid and is held in the pressure sleeve using a locking nut (21). Pressure is applied to the Teflon cup using a hydraulic ram traveling through a hollow locking nut and subsequently advancing a sapphire piston (8mm diameter x 25mm length) from the opposite end of the cell. The piston-side locking nut secures the advancing piston, allowing for the cell to remain pressurized when separated from the hydraulic press. The compression of the Teflon cap and fluid allow for the application of hydrostatic pressure on the sample. Cell pressure was determined from the applied hydraulic pressure that was calibrated in separate runs using known pressure dependence of the electrical resistance of a manganin wire (22). The loaded pressure cell is placed in the NMR probe (Fig. S2) and positioned such that the coil is perpendicular to the applied external magnetic field.

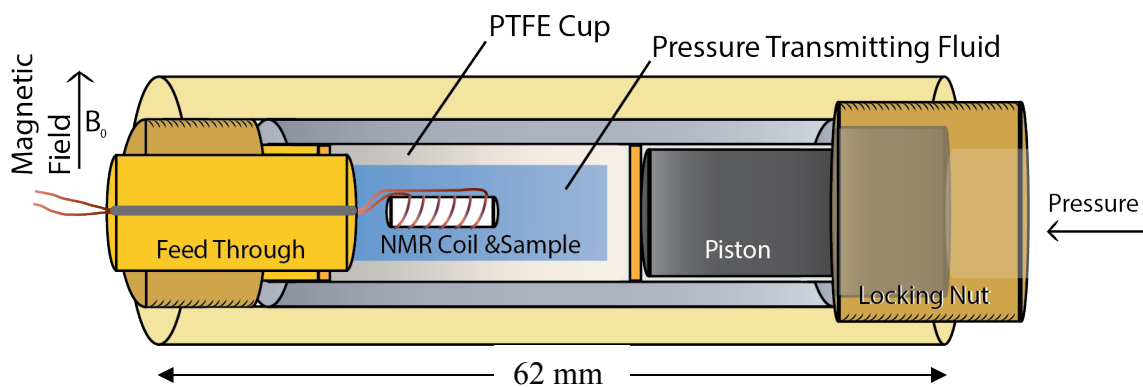


Figure S1. Pressure cell schematic. External pressure is applied to advance a piston and compress a PTFE cup containing a pressure transmitting fluid. A sample suspended in the fluid experiences hydrostatic pressure and a custom NMR coil placed around the sample allow for in-situ HP-NMR experiments. All component materials are chosen such that the pressurizing cell is completely non-magnetic. **Cell components shown are not to scale.*

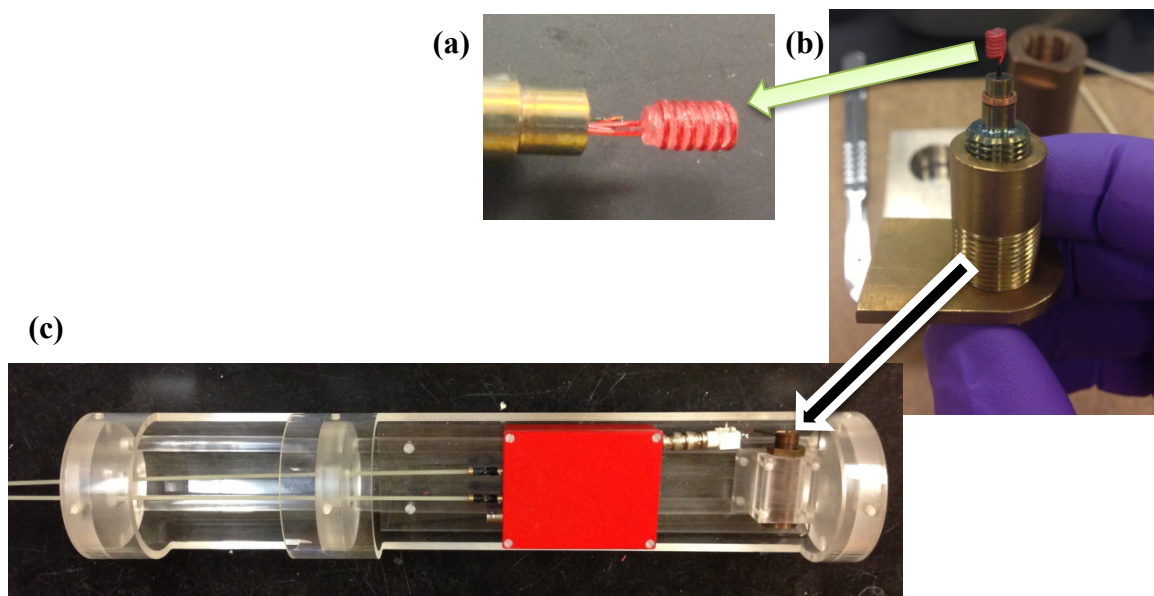


Figure S2. a) Sample glass rod fitted with a coil, (b) epoxied into the high pressure feed-through of the pressure cell and (c) loaded cell fitted to home-built NMR probe

***Ex situ* experiments in Multi-anvil cell**

In the case of the multi-anvil cell experiments, glass samples were taken in graphite capsule within an 8 mm truncated edge length castable MgO ceramic octahedron. The capsule also served as a resistance heater for high temperature experiment where the sample temperature was monitored by a Type D (W3%Re - W25%Re) thermocouple and pressure was determined using fixed-point pressure standards based on phase transitions in crystalline Bi and ZnTe.

***Ab initio* calculations of ^{11}B NMR parameters**

Ab initio calculations of ^{11}B NMR parameters were carried out on a molecule of H_3BO_3 , as a function of systematic changes in the position of the central B atom, using density functional theory (DFT) within the Gaussian 09 program package (23). The 6-311+G(d,p) basis sets based on Becke's three-parameter hybrid method with the LYP correlation (B3LYP) were used (24,25). The corresponding ^{11}B NMR parameters were computed using the continuous set of gauge transformations (CSGT) method (26-28). The experimental ^{11}B isotropic chemical shift $\delta_{\text{iso}} = 19.6$ ppm was used as reference for the fully optimized structure of the H_3BO_3 molecule.

The effects of three types of deformation of the B coordination geometry on the ^{11}B NMR parameters are considered. In the case of **Model 1**, a uniform compression/expansion of the B-O coordination triangle is considered (Fig. S3). The corresponding ^{11}B NMR parameters for the H_3BO_3 molecule as a function of B-O bond length are listed in Table S3.

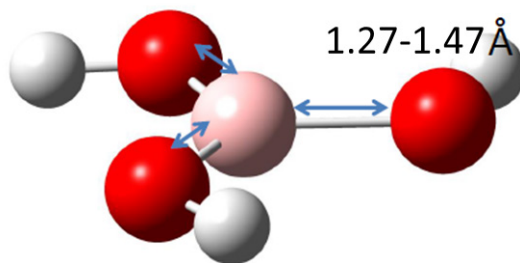


Figure S3. Uniform compression/expansion of BO_3 triangle in Model 1.

Table S3. Calculated ^{11}B NMR parameters for the H_3BO_3 molecule as a function of B-O bond length, upon deformation according to Model 1.

B-O bond length (Å)	C_Q (MHz)	η	δ_{iso} (ppm)
1.27	2.49	0.0	12.9
1.32	2.48	0.0	17.3
1.37*	2.49	0.0	19.6
1.42	2.49	0.0	24.7
1.47	2.45	0.0	28.2

* *Fully optimized equilibrium (undeformed) structure*

In the case of **Model 2**, the BO_3 environment was deformed in an anisotropic fashion where one of the B-O distances was systematically increased from 1.37 to 1.47 Å while the other two distances were allowed to relax within the B-O plane to a minimum energy configuration. (Fig. S4). The corresponding ^{11}B NMR parameters for the H_3BO_3 molecule as a function of the unique B-O bond length are listed in Table S4.

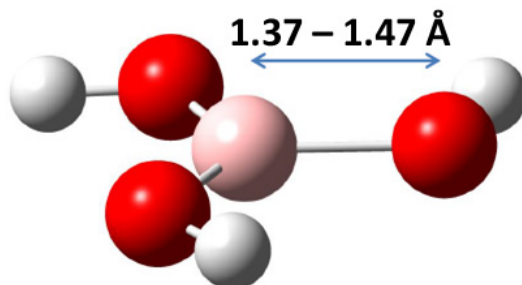


Figure S4. In-plane displacement of the B atom according to Model 2.

Table S4. Calculated ^{11}B NMR parameters for the H_3BO_3 molecule as a function of the unique (long) B-O bond length, upon deformation according to Model 2.

B-O bond length (Å)	C_Q (MHz)	η	δ_{iso} (ppm)
1.37*	2.49	0.0	19.6
1.42	2.48	0.0	20.6
1.47	2.45	0.0	21.5

* Fully optimized equilibrium (undeformed) structure

In the case of **Model 3**, the central B atom is moved vertically out of the plane of the oxygen atoms along the threefold symmetry axis and all three B-O distances were allowed to relax (Fig. S5). The corresponding ^{11}B NMR parameters for the H_3BO_3 molecule as a function of the vertical distance of the B atom from the oxygen plane and of the average B-O bond length are listed in Table S5.

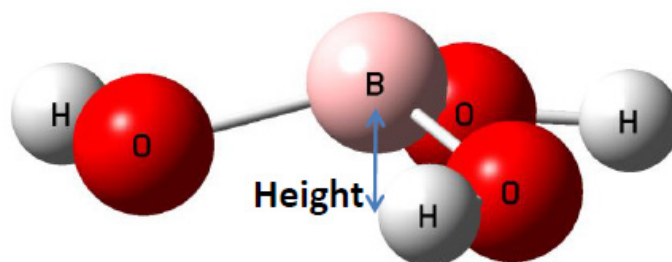


Figure S5. Vertical displacement of the B atom from the oxygen plane along the C_3 axis, in Model 3.

Table S5. Calculated ^{11}B NMR parameters for the H_3BO_3 molecule upon deformation according to Model 3.

Vertical height of B above O_3 plane (Å)	B-O bond length (Å)	C_Q (MHz)	η	δ_{iso} (ppm)
0.000*	1.370	2.49	0.0	19.6
0.196	1.374	2.47	0.0	20.4
0.279	1.379	2.44	0.0	21.4
0.345	1.385	2.43	0.0	22.6

* Fully optimized equilibrium (undeformed) structure

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